## THE DISCOVERY OF CHARGE -CONJUGATION PARITY ASYMMETRY

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by

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Physics as a science has made incredible progress because of the delicate interplay between theory and experiment. Astonishing predictions based on theories devised to account for known phenomena have been confirmed by experiment. Experiments probing previously unexplored areas often reveal physical effects which are completely unanticipated by theoretical conjecture. The incorporation of the new effects into a theoretical framework then follows.

This year Prof. Cronin and I are being honored for a purely experimental discovery, a discovery for which there were no precursive indications, either theoretical or experimental. It is a discovery for which after more than 16 years there is no satisfactory accounting. But showing as it does a lack of charge-conjugation parity symmetry and, correspondingly, a violation of time-reversal invariance, it touches on our understanding of nature at its deepest level.

The discovery of failure of CP symmetry was made in the system of K mesons. This observation is especially interesting because it was the study of these same particles that led to the overthrow of parity conservation, the notion that interactions and their mirror-reflected counterparts must be equal.

My own interest in K particles started in 1952-53 while I was at Columbia working with Jim Rainwater on  $\mu$ --mesonic atoms. At that time the strange behavior of the particles newly discovered in cosmic rays<sup>(1)</sup> was a major topic of conversation in the corridors and over coffee. By strange behavior I am referring to the copious production but slow decay. Protons bombarded by pions would result in the production of  $\Lambda^{(1)}$ 's at  $10^{13}$  times the rate of their decay back to pions and protons. Pais came to Columbia and talked of his ideas on associated production to explain this anomaly.<sup>(2)</sup> Gell Mann visited and discussed the scheme which he and independently, Nakano and Nishijima, had devised to account for associated production.<sup>(54)</sup>

Their idea was implausible and daring in the face of available data. The scheme assigned the K mesons to two doublets,  $K^*K^0$ , and the antiparticles  $K^-$  and  $\overline{K}^0$ . The natural assignment would have been the same as for pions, a triplet of particles  $K^+, K^0, K^-$ . Nishijimaalso assigned quantum numbers, subsequently called stangeness, which were conserved in the strong interaction but not in the weak. The  $K^+K^0$  were assigned + 1, the  $\overline{K}^0K^-$  as well as the  $\Lambda^0$ , - 1

Standing alone among the particles with positive strangeness were the K<sup>+</sup> and K<sup>0</sup> mesons, and I idly thought that if the situation was ever to be understood these objects might be the key. Most often experiments in physics are long and difficult. It takes some special tweaking of interest to make the commitment to a new area of research. The original motivation is, in the end, apt to appear naive. However, I did in fact join the Princeton Cosmic Ray Group headed by George Reynolds, and spent the summer of 1954 on a mountain in Colorado learning about the ongoing experiments. During the same period the energy of the cosmotron at Brookhaven was being raised to 3 GeV. Associated production was clearly seen by Shutt and his group at Brookhaven( and K mesons produced in the cosmotron were identified in photographic emulsion.<sup>(6)</sup> By the end of the summer I reluctantly decided the future was not in studying cosmic rays in the mountains I loved, but with the accelerators.

The following fall, with Bob Motley, a graduate student, we began to design an apparatus to detect K mesons using purely counter techniques at the cosmotron. As this work progressed the cascading interest in the tau-theta puzzle <sup>(7)</sup>led us naturally to explore the lifetime of the K particles as a function of their decay mode. We were successful with our detectors and Motley and I published our results simultaneously with those from the Alvarez group at Berkeley which was using the bevatron as a source. <sup>(8,9)</sup> These results showed the degeneracy in the lifetime of the tau and theta mesons. Independently the masses of tau and theta had been shown to be the same to within 1%. <sup>(10)</sup> The situation then set the stage for the famous work of Lee and Yang<sup>(11)</sup> followed by the experiments with the striking results showing maximal parity violation in the weak interactrons.<sup>(12)</sup> This remarkable story was told by Lee and Yang on this occasion in 1957.

At about this time there appeared a paper by Landau written before the results of the beta decay experiments were known.<sup>(13)</sup> Addressing the tautheta problem, he observed that a simple rejection of parity conservation would create difficult problems in physics. However, with what he called "combined inversion", that is, space inversion and the simultaneous transformation of particle into antiparticle, the difficulties would be avoided. Indeed, this is a path that nature appeared to take. Subsequent experiments showed parity violation was compensated by a failure of charge conjugation. The weak interactions were therefore invariant under the combined operations of particle-antiparticle interchange and mirror reflection, charge conjugation-parity, CP.

One symmetry had been shown to be invalid but had been replaced by a still deeper one. This new symmetry was especially appealing because of the CPT theorem. This theorem, which is based on little more than special relatively and locality and which is the foundation of all quantum field theory, says that all interactions must be invariant under C, P, and T, time reversal, all combined. If CP is good so also is T, in complete accord with all experimental data. The subject was left in a highly satisfactory state. "Who would have dreamed in 1953 that studies of the decay properties of the K particles would lead to a new revolution in our understanding of invariance principles," wrote Sakurai in 1963.<sup>(14)</sup> But then in 1964 these same particles, in effect, dropped the other shoe.

It is difficult to give a better example of the mutually complementary roles of theory and experiment than in telling the story of the neutral K mesons. For a physicist the pleasures are special because there is scarcely a physical system which contains so many of the elements of modern physics. Two-state systems, of which this is an example, abound, but this one has special properties which give it a unique beauty. I hope that I can convey to you some of the reasons why this system has held such a fascination for us. The story begins with the isotopic spin, strangeness assignment of Gell Mann and Nishijima. The assignment of the K mesons to two doublets makes the K and  $\overline{\mathrm{K}}^{_{0}}$  distinct entities. But both particles decay to two  $\pi$  mesons. If the physicist sees  $\pi^{+}$  and  $\pi$ -mesons in his detector, which is the source, the K<sup>0</sup> or  $\overline{K}^{0}$ ? The problem was solved through the remarkable insight of Gell Mann and Pais in their 1955 paper.<sup>(15)</sup> In the spirit of quantum mechanics it is necessary that the source of the  $\pi^{\dagger}\pi^{-}$  mesons be some linear combination of K<sup>0</sup> and  $\overline{K}^{0}$  states. They observed that a  $\pi^*\pi^-$  final state is even under charge conjugation. By even we mean that the wavefunction does not change its algebraic sign upon interchange of particle and antiparticle. This evenness condition is obviously met by the combination  $K^0 + \overline{K}^0$ . This they called the  $K_1^{0}$  (16) If this is the case, there must be another state equally probable, the  $K^0 - \overline{K}^0$ , the  $K^0_2$ , which is odd under charge conjugation and, correspondingly, is forbidden to decay to  $\pi^+\pi^-$ . But it can decay to many other states, three-body states such as  $\pi^+\pi^-\pi^0$  It was expected that the decay to the three-body states would be substantially inhibited compared to the two-body. The particle corresponding to the  $K_2^0$  would have a longer lifetime than the  $K_1^0$  by about 500. In addition, it was expected that the  $K_1^0$  and  $K_2^0$  would have somewhat different masses even though the masses of K" and  $\overline{K}^0$  are strictly equal by the CPT theorem.

This long-lived neutral K meson, predicted by Gell-Mann and Pais, was then looked for and found by a Columbia group working at the Brookhaven cosmotron.<sup>(17)</sup> The theoretical model, based on the notion of charge conjugation invariance in the weak interactions, had been confirmed. Then suddenly parity was found to be violated in the weak interactions along with charge conjugation! This dark cloud was almost immediately removed with the observation that one had only to replace C with CP and the story of the neutral K mesons would remain the same.<sup>(13)</sup> With CP invariance the  $K_2^0$  would continue to be absolutely forbidden to decay to two pions. The successful1 description of the neutral system of K mesons has been characterized by Feynman as "one of the greatest achievements of theoretical physics."<sup>(18)</sup>

Additional features of the  $\mathbf{K}^0 \overline{\mathbf{K}}^0$  system become evident if we write the wavefunction including the lifetime and energy terms for the case of production of a  $\mathbf{K}^0$  at t = 0.

$$\begin{split} \Psi(t) &= \frac{1}{\sqrt{2}} \left\{ |K_1^0 > e^{-t/2\tau_1 + i\omega_1 t} + |K_2^0 > e^{-t/\tau_2 + i\omega_2 t} \right\} \\ &|K_1^0 > = \frac{1}{\sqrt{2}} [|K^0 > + |\overline{K}^0 >] \\ &|K_2^0 > = \frac{1}{\sqrt{2}} [|K^0 > - |K^0 >] \end{split}$$

It is seen that after a time, long compared to the  $K_1^0$  lifetime and short compared to the  $K_2^0$  lifetime, the state that was originally a pure  $K^0$  will become a  $K_2^0$ which in turn is an equal mixture of  $K^0$  and  $\overline{K}^0$ . To give a measure of the magnitudes involved we should point out that the  $K_1^0$  meson, in a typical experimental situation, travels an average of a few centimeters before it decays, whereas the  $K_2^0$  travels tens of meters. At a distance greater than about one meter from the point of production of a  $K^0$  a nearly pure  $K_2^0$  beam will be present.

Another important characteristic of the system becomes apparent when we consider the interaction of  $K_2^{0*}s$  with matter. The  $K^{0*}s$  and  $\overline{K}^{0*}s$ , by virtue of their opposite strangeness, have quite different interaction cross sections. Passing a beam of  $K_2^{0*}s$  through a block of material will result in a mixture of  $K^0$  and  $\overline{K}^{0*}s$  which, because of differential absorption of the two components, is no longer 50-50, but instead a mixture equivalent to a new combination of  $K_1^{0*}s$  and  $K_2^{0*}s$ . The newly produced short-lived  $K_1^{0*}s$  decaying to  $\pi^*\pi^-$ will appear behind the material. This phenomenon is called regeneration.<sup>(9)</sup> In the case of the absorbing material being completely transparent to  $K^{0*}s$  and opaque to  $\overline{K}^{0*}s$  the intensity of the  $K_1^{0*}s$  after the absorber will be 1/4 the initial intensity of the  $K_2^0$  incident on the absorber.

In the late 1950's M. L. Good<sup>(20)</sup> observed that with a very small mass difference between the  $K_1^0$  and  $K_2^0$  the regeneration phenomena just discussed would result in a coherent process. By coherent we mean that the scattering process of  $\mathbf{K}_2^0$  to  $\mathbf{K}_1^0$  would not be from individual nuclei but from the whole block of scattering material! That is, the block of material would remain in its initial quantum mechanical state during the scattering process. In this case, as with ordinary light passing through glass, the regeneration material could be treated as having an index of refraction. The  $K_1^0$ 's regenerated coherently would have precisely the same energy as the incident  $K_2^{0,s}$  and an angular distribution identical to the incident beam but broadened by diffraction effects determined by the size of the regenerating material perpendicular to the beam. A characteristic wavelength for the  $\mathbf{K}_{2}^{0}$  mesons in a typical experiment is about 10113 cm. The transverse dimensions are typically 10 cm. The corresponding diffraction pattern has a width of the order of 10<sup>-14</sup> radians! In addition, the coherent addition of  $K_1^0$  waves has been observed over distances greater than 10<sup>14</sup> wave lengths. The unique feature of this coherently regenerated  $K_1^0$  beam is that it can be distinguished from the original beam since it decays with a short lifetime to  $\pi^+ \pi^-$ . To my knowledge, it is the only instance where a forward coherently scattered beam can be distinguished from the original beam.

It has become evident to physics students in the audience that the  $K_1^0 K_2^0$ story has an analogy in polarized light. The  $K_1^0$  and  $K_2^0$  correspond to the left and right circularly polarized light, and the  $K^0$  and  $\overline{K}^0$  states are equivalent to the x and y components of linear polarization. The passage of a  $K_2^0$  beam through a block of condensed material is equivalent to the passage or left circular polarized light through a doubly refractive medium like calcite which has a different index refraction for the x and y components of polarization. The general picture of regeneration, coherent and incoherent, was confirmed in a definitive bubble chamber experiment.<sup>(21)</sup> There are many associated phenomena still to be explored. For example, experiments coherently regenerating  $K_1^{0,s}$  from the planes in crystals have yet to be done. At the particle momenta commonly available the Bragg angles are exceedingly small, and the extinction factor, the Debye-Waller factor, comes into play at correspondingly small angles, but the experiments could be done.

Unexpectedly, the K"  $\overline{\mathbf{K}}^0$  system provides us with important and highly precise information about the gravitational interaction. It relates to the question of strong universality; that is, whether different objects, in this case particle and antiparticle, with the same inertial mass behave the same in a gravitational field. As observed by M. L. Good,<sup>(22)</sup> if the K" and its antiparticle, the  $\overline{\mathbf{K}}^0$ , had an opposite gravitational potential energy, the K"  $\overline{\mathbf{K}}^0$  system would mix so quickly that the long-lived particle would never be seen. By analyzing the system in more detail one can show that if the gravitational interaction of particle and antiparticle differ by a fraction,  $\kappa$ , then  $\kappa$  must be less than 10<sup>-10</sup> if we're dealing with the gravitational field of the earth, 10<sup>-11</sup> for the solar system, and 10<sup>-13</sup> for the galaxy.

Voyages of discovery can be made in new uncharted waters but also in the familiar bays close to port provided one has observing apparatus that can see familiar objects with detail greater than that previously possible. In 1963 we had the opportunity to investigate the neutral K meson phenomena with resolution greater than that permitted before. The introduction of spark chambers as charged particle detectors permitted precise track position determination, but also the chambers could be selectively triggered on appropriate classes of events.

Using such new devices with our colleagues, Jim Christenson and Rene Turlay, Jim Cronin and I initiated a systematic study of (1) the regeneration phenomena, (2) what we called CP invariance, and (3) neutral currents. We were interested in the regeneration phenomena in particular because of an anomaly that had just been reported by a group studying the passage of  $K_2^{0,s}$  sthrough a liquid hydrogen bubble chamber.<sup>(2)</sup> Not many of our colleagues would have given us much credit for studying CP invariance, but we did anyway, and neutral currents, of long interest, were discussed by Professor Glashow on this occasion one year ago.

A plan view of the apparatus we used for these studies is shown in Figure 1. It is a two-armed spectrometer, each arm with spark chambers before and after a magnet for track delineation. Cerenkov and scintillation counters in both arms operated in coincidence provided the signals to trigger the spark chambers, which were recorded photographically. The apparatus was placed in a beam of neutral particles at the Brookhaven A. G. S. at a distance such that  $K_1^{0}$ 's would have decayed away leaving  $K_2^{0}$ 's. The angle between the spectrometer arms was chosen to optimize the detection of K" mesons decaying to two  $\pi$  mesons. In the regeneration studies blocks of various solid materials were placed in the neutral beam. In the studies of the free decay of  $K_2^0 \rightarrow 2$  pions, the decay volume was filled with helium gas to minimize the interactions.

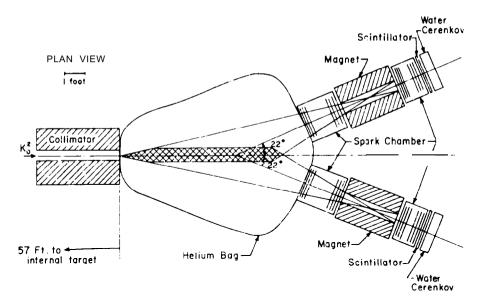


Fig. I. Plan view of the apparatus as located at the A. G. S.

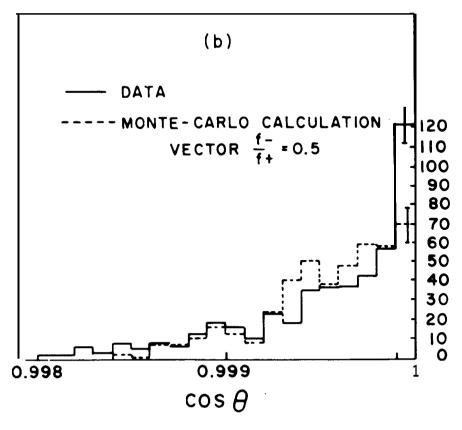


Fig. 2. Angular distributions of those events in the appropriate mass range as measured by a coarse measuring machine.

The decay to 2 pions is distinguished from the copious three-body decays in two ways. The sum of the momenta of the two detected particles must line up with the direction of the incident  $\mathbf{K}_{2}^{0,s}$ . In general this will not happen for three-body decay. In addition, the mass computed for the parent particle must match the mass of the  $K^0$  meson. The original data are shown in Figure 2 and 3. Figure 2 shows the data after measurement of the photographic records on a relatively coarse measuring machine. The presence of the peaking of events along the beam line stimulated more precise measurements and these results are shown in Figure 3. Clearly there are about 56 events in the forward peak in the proper mass interval where the background is 11. From this data we established that the branching ratio of  $\mathbf{K}_2^0$  to 2 pions relative to all the charge modes decay was 2x 10<sup>-3</sup>. Here was the first evidence for the decay completely forbidden by CP conservation.<sup>(23)</sup>We were acutely sensitive to the importance of the result and, I must confess, did not initially believe it ourselves. We spent nearly half a year attempting to invent viable alternative explanations, but failed in every case.

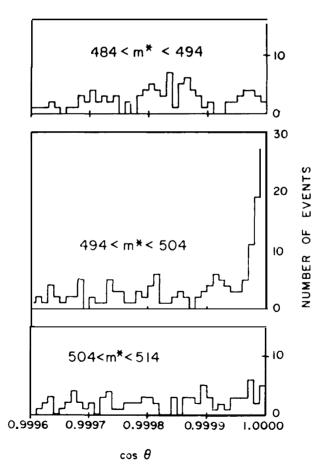


Fig. 3. Angular distribution of the events after measurement by a precise machine in three relevant mass regions.

The study of coherent regeneration was important for the CP measurement for several reasons. First, the results we found were entirely consistent with expectations; there were no anomalies. The measured coherent regeneration rates in tungsten, copper, carbon, and liquid hydrogen enabled us to show that coherent regeneration in the gaseous helium which filled the decay volume would produce a totally negligible contribution to the signal we observed. Second, the coherent regeneration of the  $K_1^0$ 's, which subsequently decrayed to  $\pi^*\pi^-$ mesons, provided an invaluable calibration of the apparatus.

It is appropriate now to look at the neutral K system in a somewhat more quantitative way.<sup>24</sup>Because of the mixing of the  $K^0$  and  $\overline{K}^0$  through the weak interaction, the time rate of change of a  $K^0$  wave will not only depend on the  $K^0$  amplitude, but also on the  $\overline{K}^0$  amplitude, viz.,

and 
$$-\frac{\mathrm{d} \mathbf{K}^{0}}{\mathrm{d} \mathbf{t}} = \mathbf{A} \mathbf{K}^{0} + \mathbf{p}^{2} \overline{\mathbf{K}}^{0}$$
$$-\frac{\mathrm{d} \overline{\mathbf{K}}^{0}}{\mathrm{d} \mathbf{t}} = \mathbf{B} \overline{\mathbf{K}}^{0} + \mathbf{q}^{2} \mathbf{K}^{0}.$$

We have let the particle symbol stand for the amplitude of the corresponding wave. With invariance under CPT, particle and antiparticle masses and lifetimes must be precisely identical. In terms of the above equations, A must be equal to B. Now, CP violation can, in fact, occur in two ways, either through terms in the set of equations above, or in the amplitudes for the decay. Subsequent experiments show that most, if not all, of the violation is in the equations above, involving the so-called mass-decay matrix. Professor Cronin will discuss the ramifications of the effect being present also in the decay terms. Suffice is to say here that any departure of p<sup>2</sup> from q<sup>2</sup> will result in the decay of the  $K_2^0 \rightarrow 2$  pions. With CP nonconservation the short and longlived particles are no longer the  $K_1^0$  and  $K_2^0$  previously defined but rather

and

$$\begin{split} & K_{S}^{0} = \frac{l}{\sqrt{p^{2} + q^{2}}} \quad \{p|K^{0} > + q|\overline{K}^{0} > \} \\ & K_{L}^{0} = \frac{l}{\sqrt{p^{2} + q^{2}}} \quad \{ p|K^{0} > - q|\overline{K}^{0} > \} \end{split}$$

The fact that  $K^0_L$  decays to 2 pions shows that the amplitude for particle to antiparticle transitions, in this case  $K^0 \rightarrow \overline{K}^0$ , does not quite equal the reverse,  $\overline{K}^0 \rightarrow K^0$ , and indeed we now know rather precisely that not only are the magnitudes somewhat different but that there is a small phase angle between the two amplitudes. See Figure 4.

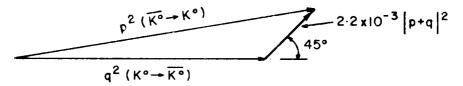


Fig. 4. Vector diagram showing schematically the difference in the amplitudes for  $K^0 \rightarrow \overline{K}^0$  and  $\overline{K}^0 \rightarrow K^0$ .

We indicated earlier that, through the CPT theorem, a violation of CP is equivalent to a violation of time reversal invariance. As Professor Cronin will show, the CPT theorem has been shown to hold in the neutral K system independently, so in a self-contained way a violation of time reversal invariance is demonstrated.

We are all familiar with the time asymmetry associated with entropy. Entropy in a closed system increases with time. This kind of time asymmetry results from the boundary conditions. But for the first time we have in the neutral K mesons a physical system that behaves asymmetrically in time as a result of an interaction, not a boundary condition.

Since the microscopic physical laws had always been thought to be invariant under time reversal, this discovery opens up a very wide range of profound questions. Professor Cronin will go into some of these questions in greater detail. I will mention two. Can this effect be used to decrease the entropy of an isolated system? We look out from the earth and see a highly ordered universe. With entropy always increasing how can this be? Is CP violation an effect that can be used, in effect, to wind up the universe? The answers to these questions appear to be no.<sup>(25)</sup>

At the same time we look out from the earth and see the remains of an earlier much hotter universe. In that earlier time one expects that matter and antimatter would condense out in equal amounts and eventually annihilate to gamma radiation. However no evidence of antimatter is seen. The gauge theories described on this occasion one year ago allow for the possibility of proton (and antiproton) decay. This process, coupled with CP violation, drives the universe towards a preponderance of matter over antimatter and can account for the observed ratio of the amount of matter to radiation.<sup>(20)</sup>

Lewis Thomas, whose essays on science grace our literature, has written, "You measure the quality of the work by the intensity of the astonishment." After 16 years, the world of physics is still astonished by CP and T non-invariance. I suspect that the Nobel Committee was motivated by considerations similar to those of Thomas in awarding to Professor Cronin and myself this highest of honors.

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- Among the strange particles some were seen to decay to two and some to three pions. By using the analysis of Dalitz and Fahri, it was shown, with very few examples in hand, that the parity of the three pion system was opposite to that of the two pion system. If parity is conserved in the decay interaction then there must he distinguishable parents of opposite parity, the theta that decays to two and the tau that decays to three pions. The puzzle was in the question, if the particles are distinct entities why should they have the same mass and lifetime? Now with parity violation both are recognized as K mesons,  $K_{\pi 2}$  and  $K_{\pi 3}$ .
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